| Question | Answer | Marks | Guidance |
|---------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1 (i) (ii) | $P(X = 0) = 0.4 \times 0.5^{4} = 0.025$ $\underline{NB \text{ ANSWER GIVEN}}$ $P(X = 1) = (0.6 \times 0.5^{4}) + (4 \times 0.4 \times 0.5 \times 0.5^{3})$ $= 0.0375 + 0.1 = 0.1375$ $\underline{NB \text{ ANSWER GIVEN}}$ | M1 A1 [2] M1* M1* M1* dep A1 [4] | For 0.5^4 For 0.6×0.5^4 seen as a single term (not multiplied or divided by anything) For $4 \times 0.4 \times 0.5^4$ Allow 4×0.025 Watch out for incorrect methods such as (0.4/4) 0.1 <u>MUST</u> be justified For sum of both , dep on both M1's |
| (iii) | $ \begin{array}{c} 0.35 \\ 0.3 \\ 0.25 \\ 0.2 \\ 0.15 \\ 0.1 \\ 0.05 \\ 0 \\ 0 \\ 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ r \\ \end{array} $ | G1 G1 [2] | For labelled linear scales on both axes Dep on attempt at vertical line chart. Accept P on vertical axis For heights – visual check only but last bar taller than first and fifth taller than second and fourth taller than third. Lines must be thin (gap width > line width). All correct. Zero if vertical scale not linear Everything correct but joined up tops GOG1 MAX Everything correct but f poly GOG1 MAX Everything correct but bar chart GOG1 MAX Curve only (no vertical lines) gets GOG0 Best fit line GOG0 Allow transposed diagram |

| C | Questio | n | Answer | Marks | Guidance |
|---|---------|---|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1 | (iv) | | 'Negative' or 'very slight negative' | E1 [1] | E0 for symmetrical but E1 for (very slight) negative skewness even if also mention symmetrical Ignore any reference to unimodal |
| | (v) | | $E(X) = (0 \times 0.025) + (1 \times 0.1375) + (2 \times 0.3) + (3 \times 0.325) + (4 \times 0.175) + (5 \times 0.0375) = 2.6$ | M1 A1 | For Σrp (at least 3 terms correct) CAO |
| | | | $E(X^{2}) = (0 \times 0.025) + (1 \times 0.1375) + (4 \times 0.3) + (9 \times 0.325) + 16 \times 0.175) + (25 \times 0.075) = 0 + 0.1375 + 1.2 + 2.925 + 2.8 + 0.9375 = 8$ | M1* | For $\Sigma r^2 p$ (at least 3 terms correct) |
| | | | $Var(X) = 8 - 2.6^2$ | M1* dep | for – their E(X) ² |
| | | | = 1.24 | A1 [5] | FT their E(X) provided Var(X) > 0 USE of E(X- μ) ² gets M1 for attempt at $(x-\mu)^2$ should see (- 2.6) ² , (-1.6) ² , (-0.6) ² , 0.4 ² , 1.4 ² , 2.4 ² (if E(X) correct but FT their E(X)) (all 5 correct for M1), then M1 for $\Sigma p(x-\mu)^2$ (at least 3 terms correct) Division by 5 or other spurious value at end gives max M1A1M1M1A0, or M1A0M1M1A0 if E(X) also divided by 5. Unsupported correct answers get 5 marks. |
| | (vi) | | $\begin{array}{l} P(\text{Total of } 3) = (3 \times 0.325 \times 0.025^2) + (6 \times 0.3 \times 0.1375 \times 0.025) + \\ 0.1375^3 = 3 \times 0.000203 + 6 \times 0.001031 + 0.002600 = \\ 0.000609 + 0.006188 + 0.002600 = 0.00940 \end{array}$ | M1 M1 | For decimal part of first term 0.325×0.025^2 For decimal part of second term $0.3 \times 0.1375 \times 0.025$ |
| | | | (= 3×13/64000 + 6×33/32000 + 1331/512000) | M1 A1 [4] | For third term – ignore extra coefficient All M marks above depend on triple probability products CAO: AWRT 0.0094. Allow 0.009 with working. |

| 2 (i) | Median = 2 Mode = 1 | B1 CAO B1 CAO | 2 |
|----------|------------------------|---------------------------------------------------------|---|
| (ii) | 60 | S1 labelled linear scales on both axes H1 heights | 2 |
| (iii) | Positive | B1 | 1 |
| | | TOTAL | 5 |

| 3 (i) | Positive | B1 | 1 |
|----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------|
| (ii) | Number of people = 20 × 33 (000) + 5 × 58 (000) = 660 (000) + 290 (000) = 950 000 | M1 first term M1(indep) second term A1 cao NB answer of 950 scores M2A0 | 3 |
| (iii) | (<i>A</i>) $a = 1810 + 340 = 2150$ (<i>B</i>) Median = age of 1 385 (000 th) person or 1385.5 (000) Age 30, cf = 1 240 (000); age 40, cf = 1 810 (000) Estimate median = (30) + $\frac{145}{570} \times 10$ Median = 32.5 years (32.54) If no working shown then 32.54 or better is needed to gain the M1A1. If 32.5 seen with no previous working allow SC1 | M1 for sum A1 cao 2150 or 2150 thousand but not 215000 B1 for 1 385 (000) or 1385.5 M1 for attempt to interpolate $\frac{145k}{570k} \times 10$ (2.54 or better suggests this) A1 cao min 1dp | 2 3 |
| (iv) | Frequency densities: 56, 65, 77, 59, 45, 17 (accept 45.33 and 17.43 for 45 and 17) | B1 for any one correct B1 for all correct (soi by listing or from histogram) | |
| | | Note: all G marks below <i>dep</i> on attempt at frequency density, NOT frequency G1 Linear scales on both axes (no inequalities) G1 Heights FT their listed fds or all must be correct. Also widths. All blocks joined | |
| | | G1 Appropriate label for vertical scale eg 'Frequency density (thousands)', 'frequency (thousands) per 10 years', 'thousands of people per 10 years'. (allow key). OR f.d. | 5 |

| (v) | Any two suitable comments such as: | E1 | |
|------|-------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------|----|
| | Outer London has a greater proportion (or %) of people under 20 (or almost equal proportion) | E1 | |
| | The modal group in Inner London is 20-30 but in Outer London it is 30-40 | | |
| | Outer London has a greater proportion (14%) of aged 65+ | | |
| | <u>All</u> populations in <u>each</u> age group are higher in Outer London | | |
| | Outer London has a more evenly spread distribution or balanced distribution (ages) o.e. | | 2 |
| (vi) | Mean increase ↑ median unchanged (-) midrange increase ↑ | Any one correct B1 Any two correct B2 Any three correct B3 All five correct B4 | |
| | standard deviation increase ↑ interquartile range unchanged. (-) | | 4 |
| | | IUIAL | 20 |